**Experiment: Principal Component Analysis (PCA) vs Linear Discriminant Analysis (LDA) vs T-distributed Stochastic Neighbour Embedding (t-SNE) vs Multi-Dimensional Scaling (MDS)**

**Title:**

**Implement a Multidimensionality Scaling Algorithm**[**MDS**](https://lms.sitpune.edu.in/mod/resource/view.php?id=18926)**on a specific dataset and compare its outcomes with other dimensionality reduction techniques such as PCA LDA and T-SNE**

**Aim:**

**Comparing the results of MDS with LDA, PCA and t-SNE for better suitability**

**Objective:**

Students will learn:

* The implementation of the Multi-Dimensional Scaling, principal component analysis and Linear Discriminant analysis and T-distributed stochastic neighbour embedding on a dataset.
* Visualization and interpretation of results.

**Problem Statement**

APPLY AND IMPLEMENT MDS ALGORITHM ON A SPECIFIC DATASET OF YOUR CHOICE AND COMPARE THE OUTCOMES WITH T-SNE, PCA AND LDA FOR THE SAME

**Explanation / Stepwise Procedure / Algorithm**

### **Principal Component Analysis (PCA)**

PCA is a widely used dimensionality reduction technique that transforms high-dimensional data into lower-dimensional data while retaining most of the information. The goal of PCA is to identify the directions (principal components) in which the data varies the most and project the data onto those directions.

#### **Here's how PCA works:**

1. Standardize the data by subtracting the mean and dividing by the standard deviation.
2. Compute the covariance matrix of the standardized data.
3. Perform eigenvalue decomposition on the covariance matrix to obtain eigenvectors and eigenvalues.
4. Select the top k eigenvectors corresponding to the largest eigenvalues.
5. Project the original data onto the selected eigenvectors to obtain the lower-dimensional representation.

#### **PCA is useful for:**

* Reducing the dimensionality of high-dimensional data
* Identifying patterns and correlations in the data
* Improving the performance of machine learning algorithms

### **Linear Discriminant Analysis (LDA)**

LDA is a supervised dimensionality reduction technique that finds a linear combination of features that best separates different classes in the data. LDA is commonly used for classification problems and is particularly useful when the number of features is high and the number of samples is small.

#### **Here's how LDA works:**

1. Standardize the data by subtracting the mean and dividing by the standard deviation.
2. Compute the within-class scatter matrix and the between-class scatter matrix.
3. Perform eigenvalue decomposition on the scatter matrices to obtain eigenvectors and eigenvalues.
4. Select the top k eigenvectors corresponding to the largest eigenvalues.
5. Project the original data onto the selected eigenvectors to obtain the lower-dimensional representation.

#### **LDA is useful for:**

* Reducing the dimensionality of high-dimensional data
* Improving the performance of classification algorithms
* Identifying the most discriminative features for classification

### **t-Distributed Stochastic Neighbor Embedding (t-SNE)**

t-SNE is a non-linear dimensionality reduction technique that maps high-dimensional data to lower-dimensional data while preserving local structure. t-SNE is particularly useful for visualizing high-dimensional data and identifying patterns or clusters that may not be apparent in the original data.

#### **Here's how t-SNE works:**

1. Compute the similarity matrix of the high-dimensional data using a Gaussian kernel.
2. Convert the similarity matrix into a joint probability distribution.
3. Define a cost function that measures the difference between the joint probability distribution of the original data and the lower-dimensional representation.
4. Minimize the cost function using gradient descent to obtain the lower-dimensional representation.

#### **t-SNE is useful for:**

* Visualizing high-dimensional data in a lower-dimensional space
* Identifying patterns and clusters in the data
* Reducing the dimensionality of high-dimensional data while preserving local structure

### **Multidimensional Scaling (MDS)**

MDS is a dimensionality reduction technique that represents high-dimensional data in a lower-dimensional space while preserving the pairwise distances between points as accurately as possible. MDS is particularly useful for visualizing similarity or dissimilarity data and understanding relationships between data points.

#### **Here's how MDS works:**

1. Compute the pairwise dissimilarity matrix using an appropriate distance metric (e.g., Euclidean, Manhattan).
2. Convert the dissimilarity matrix into a form suitable for eigenvalue decomposition (for Classical MDS) or define a cost function based on stress minimization (for Non-Metric MDS).
3. Perform eigenvalue decomposition or use an iterative optimization algorithm to compute the lower-dimensional representation.
4. Select the top k dimensions that best preserve the original distances.
5. Assign each data point new coordinates in the lower-dimensional space.

#### **MDS is useful for:**

* Visualizing high-dimensional data in 2D or 3D
* Understanding relationships and similarities between data points
* Reducing dimensionality while maintaining pairwise distances
* Analyzing preference or similarity data in psychology and market research

**Figures/Diagrams**

* MDS and LDA, PCA and t-SNE plots plotted for the dataset.
* Comparison between MDS, LDA,PCA and t-SNE.

A screenshot of a graph

AI-generated content may be incorrect.

A graph with red and blue lines

AI-generated content may be incorrect.A graph with blue and orange dots

AI-generated content may be incorrect.

A graph showing a diagram of cancer

AI-generated content may be incorrect.

**Challenges Encountered**

1. Parameter Sensitivity – MDS requires selecting an appropriate distance metric and the number of dimensions for embedding. Incorrect choices can lead to misleading representations.
2. Computational Complexity – Classical MDS involves eigenvalue decomposition, which can be computationally expensive for large datasets, making it slower than PCA but comparable to t-SNE.
3. Interpretability – Unlike PCA, which preserves variance, or LDA, which focuses on class separation, MDS focuses on pairwise distances, making the results harder to interpret in certain contexts.
4. Comparison with Other Techniques – MDS is an unsupervised method like t-SNE and PCA, whereas LDA is supervised. Comparing them requires analyzing both global and local structures, as well as the effectiveness of dimensionality reduction for visualization and classification.

**Conclusion**

* Implementing MDS on a specific dataset provides valuable insights into how pairwise distances are preserved in lower dimensions. However, careful selection of distance metrics is crucial for meaningful results.
* Compared to PCA, which focuses on variance maximization, and LDA, which optimizes class separation, MDS prioritizes preserving the original distance relationships, making it useful for exploratory data analysis.
* t-SNE emphasizes local structures, while MDS aims for global distance preservation, leading to different visualization outcomes.
* The choice between MDS, PCA, LDA, and t-SNE depends on the dataset and the specific goals of dimensionality reduction—whether for classification, clustering, or visualization.